

ALGEBRA 2H

Section 12.3: Combinations

NOTES

I. Combinations

Definition: A **combination** is an arrangement of objects in which the order is _____ important.

Examples:

- (a) How many different ways can the letters A, B, C be arranged if the order matters? List them.

- (b) How many different ways can the letters A, B, C be arranged if the order does not matter? List them.

- (c) How many different ways can the letters A, B, C be arranged if the order does not matter and we only use 2 out of the 3 letters? List them.

II. Combinations of n Objects Taken r at a Time

If you have n objects but you are only using r of them in your arrangement and the order of the objects does not matter (meaning that changing the order does not make a new arrangement), then it is a combination.

Formula: The combination of n objects taken r at a time, denoted _____,

is found by _____

Note: You can find these combinations with a calculator (the calculator knows the formula).

Examples:

- (a) If you have 20 books and can place 7 of them on shelf, how many different arrangements can you make if the order of the books does not matter?
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- (b) If you have 15 CD's, how many ways can you listen to 3 of them if you don't care what order they are in? _____
- (c) You are playing a card game where you will be dealt 7 cards from a standard deck of cards. How many different "hands" are possible? _____
- (d) If you have 10 people in a club and you need 4 of them to be on a committee together, how many different committees are possible? _____
- (e) If you have 10 people in a club and you need to select 4 officers (president, vice-president, secretary, and treasurer), how many different ways are possible? _____
- (f) A book store has 10 novels and 6 nonfiction books to choose from. How many ways are there to select 3 novels and 2 nonfiction books? _____

III. Using Combinations in Probability

Example: You are playing a card game where you will be dealt 4 cards from a standard deck of cards.

- (a) How many different "hands" are possible? _____
- (b) What is the probability that you have all 4 aces? _____
- (c) What is the probability that you have 2 aces and 2 kings? _____
- (d) What is the probability that you have 3 queens? _____