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## Review of Algebra 1 Factoring Notes

## Lesson \#1: Common Monomial Factoring

When two or more numbers are multiplied, the result is a single number. Factoring is the reverse process. In factoring, one begins with a single number and expresses it as a product of two or more numbers. This process also works for polynomials.

## Example \#1:

Find the GCF (greatest common factor).

1. 4 and 10
2. $36 x$ and $45 x^{2}$
3. $7 a^{4} b^{2}, 21 a^{3} b$, and $49 a^{2} b^{3}$

A polynomial that can NOT be factored is called $\qquad$ .

## Example \#2:

Tell whether or not the polynomial is prime.

1. $5 x+1$
2. $4 m^{3}+5 m^{2}$

## Example \#3:

Factor the polynomial completely

1. $7 y^{2}+3 y$
2. $4 a^{2}-50 a+10$
3. $39 m^{3}-24 m^{2}$

## Example \#4:

The area of a rectangle is $75 t^{3}-60 t^{2}+30 t$. The width is $15 t$. Find the length.

## Example \#5:

Simplify.

1. $\frac{7 s t^{2}+14 s t-49 s^{2} t}{7 s t}$
2. $\frac{m^{12}+3 m^{9}-4 m^{7}}{m^{5}}$

## Lesson \#2: Factoring Difference of Two Squares

## Multiplying Conjugates

Multiply and simplify, then look for a pattern.

1. $(x+3)(x-3)$
2. $(2 y+7)(2 y-7)$
3. $(3 a+5 b)(3 a-5 b)$

What do you notice about the outside and inside terms of the FOIL?

What do you notice about the first and last terms of the FOIL?

## Difference of Two Squares Pattern

$$
\begin{aligned}
& \begin{array}{r}
\text { Look for two perfect squares } \\
\text { being subtracted }
\end{array}
\end{aligned} \begin{aligned}
& \text { then it factors as the sum and } \\
& \text { difference of the square roots }
\end{aligned}
$$

Factor.

1. $4 x^{2}-1$
2. $25 x^{2}+81$
3. $25 m^{2} n^{2}-16$

## Lesson \#3: Factoring Trinomials of the form $a x^{2}+b x+c$

Factoring is related to multiplication, a quadratic trinomial can be factored by working backward with the FOIL method, using guess-and-check.

Factor:
a. $x^{2}+14 x+40$
b. $3 x^{2}-10 x+3$
c. $6 x^{2}+7 x-3$

Factor completely:
a. $2 x^{3}+16 x^{2}+24 x$
b. $3 x^{3} y+18 x^{2} y+27 x y$

## Lesson \#4: Solving Quadratic Equations by factoring

Quadratic Equation: $a x^{2}+b x+c=0$
** Zero Product Property

$$
\text { If } a \cdot b=0 \text {, then } a=0 \text { or } b=0 \text {. }
$$

** Example

$$
\begin{aligned}
& \text { If }(x+1)(x-2)=0 \\
& \text { then } x+1=0 \text { or } x-2=0 \\
& \text { so } x=-1 \text { or } x=2 \text { are the solutions }
\end{aligned}
$$

Solve.

1. $(x-2)(3 x+1)(x+5)=0$
2. $2 s(s+3)=0$

Factor and solve.

1. $x^{2}-10 x+9=0$
2. $x^{2}-9 x+18=0$

Set equal to zero. Factor and solve.

1. $x^{2}-16 x=36$
2. $x^{2}-7 x=-12$
3. $x^{2}=25$
